

Code MIGALE state-of-the-art

A. Colombo

HiOCFD4

4th International Workshop on High-Order CFD Method
Foundation for Research and Technology Hellas (FORTH), Heraklion (Crete)
4th June 2016



**UNIVERSITÀ DEGLI STUDI
DI BERGAMO**



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...with the contribution of

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**Towards Industrial LES/DNS in Aeronautics
Paving the Way for Future Accurate CFD
grant agreement No.635962**



Brief code summary

- Discontinuous Galerkin (DG) method on hybrid grids
- Physical frame orthonormal basis functions
- 2D/3D steady and unsteady compressible and incompressible flows
- Explicit and implicit time accurate integration
- Fixed or rotating frame of reference
- Euler
- Navier–Stokes
- RANS coupled with the k - ω (EARSM)
- Hybrid RANS/LES (X-LES)
- MPI parallelism
- Fortran language



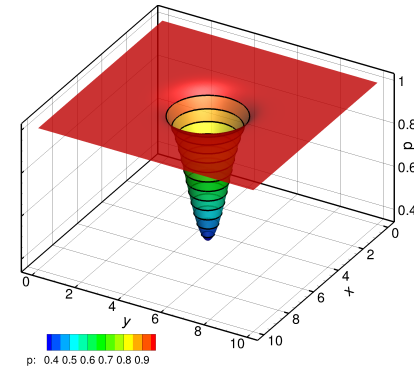
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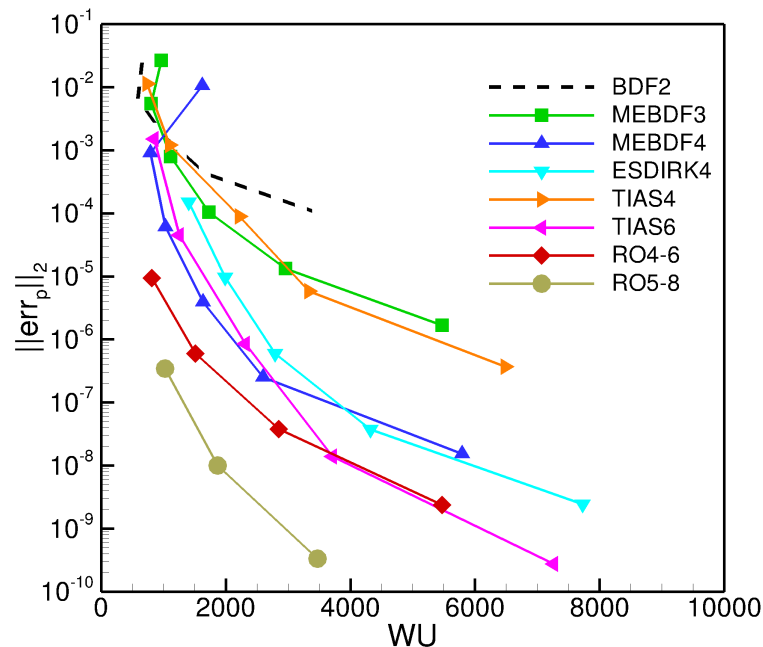
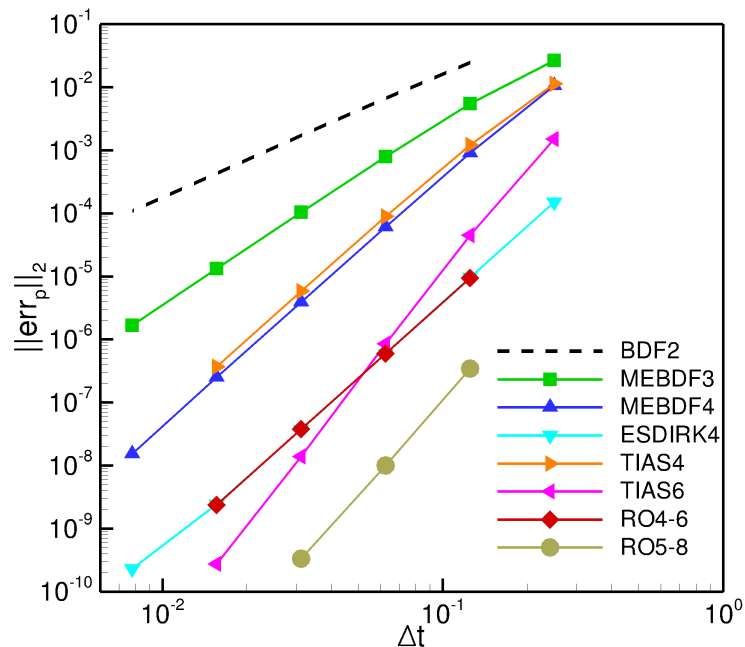
Implicit accurate time integration

Several high-order temporal schemes are implemented

- Modified Extended BDF
 - Two Implicit Advanced Step-point (TIAS)
 - Explicit Singly Diagonally Implicit R-K (ESDIRK)
 - linearly implicit Rosenbrock method
- } *non-linear systems solution*
linear systems solution (here via GMRES)



- Hi-O schemes are **more efficient** than Lo-O ones for high required accuracy
- Rosenbrock-type schemes are **appealing** both for accuracy and efficiency



Convection of
an isentropic
vortex
 P^6 solution on
50X50 el.

Rosenbrock schemes in a nutshell (I/II)

From the DG spatial discretization we obtain a system of non-linear ODEs or DAEs

$$\mathbf{M}_P(\mathbf{W}) \frac{d\mathbf{W}}{dt} + \mathbf{R}(\mathbf{W}) = \mathbf{0} \quad \tilde{\mathbf{R}} = \mathbf{M}_P^{-1} \mathbf{R}$$

$$\mathbf{W}^{n+1} = \mathbf{W}^n + \sum_{j=1}^s m_j \mathbf{Y}_j$$

$$\left(\frac{\mathbf{M}_P}{\gamma \Delta t} + \mathbf{J} - \frac{\partial \mathbf{M}_P}{\partial \mathbf{W}} \tilde{\mathbf{R}} \right)^n \mathbf{Y}_i = -\mathbf{M}_P^n \left[\tilde{\mathbf{R}} \left(\mathbf{W}^n + \sum_{j=1}^{i-1} a_{ij} \mathbf{Y}_j \right) - \sum_{j=1}^{i-1} \frac{c_{ij}}{\Delta t} \mathbf{Y}_j \right]$$

$i = 1, \dots, s$

only a **linear system** need to be solved for each stage

i.e. the **Jacobian** $\mathbf{J} = \partial \mathbf{R} / \partial \mathbf{W}$ is **assembled and factored only once per time step**

With **orthonormal basis** functions (*physical space*) $\mathbf{M}_P$ reduces to the **identity** for compressible flows with **conservative** variables

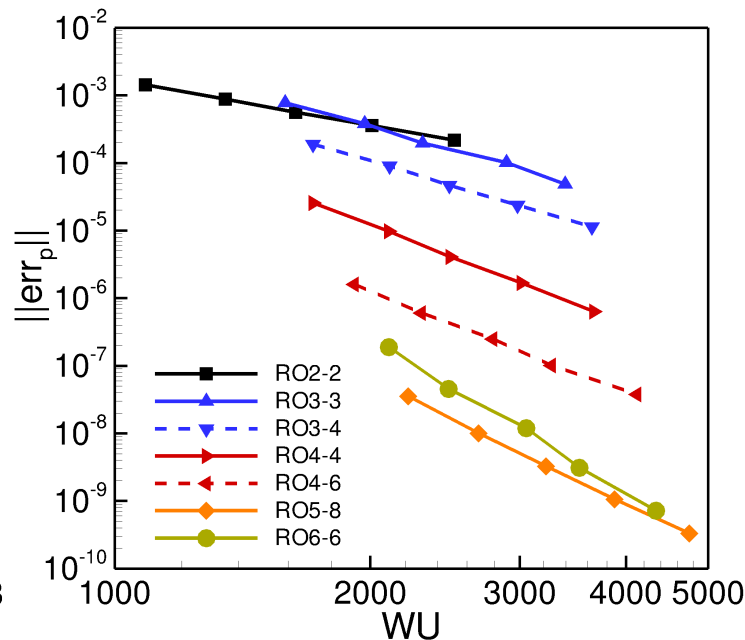
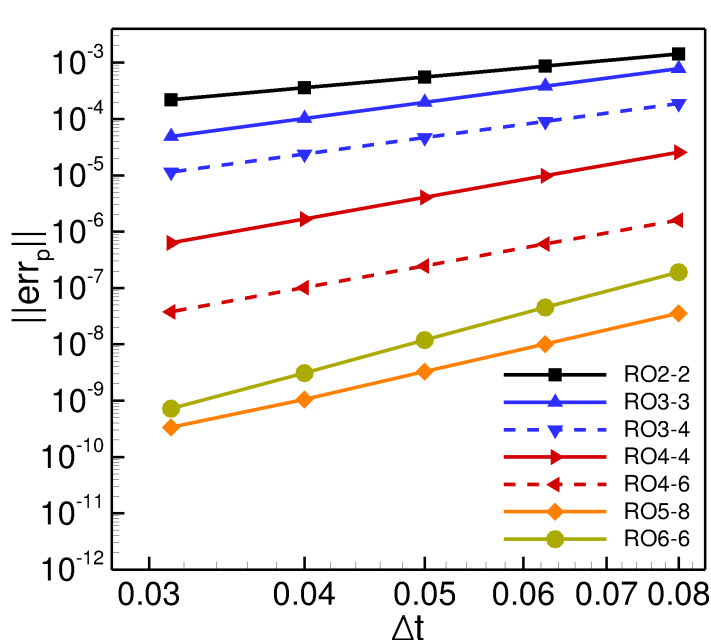
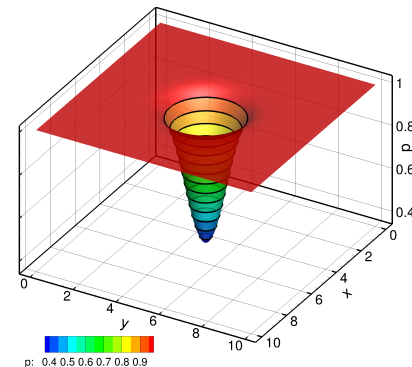
For **other sets of variables** their DOFs can be coupled within $\mathbf{M}_P$ thus resulting in a matrix which can **not** be **diagonal**

Rosenbrock schemes in a nutshell (II/II)

Several Rosenbrock schemes, from order two to order six, have been compared

No need to “exactly” solve systems: **GMRES tolerance can be increased** with confidence with a significant **reduction of WU**

For a given order of accuracy, among the schemes considered, those with **more stages are more accurate and efficient**, e.g. RO5-8 vs. RO6-6



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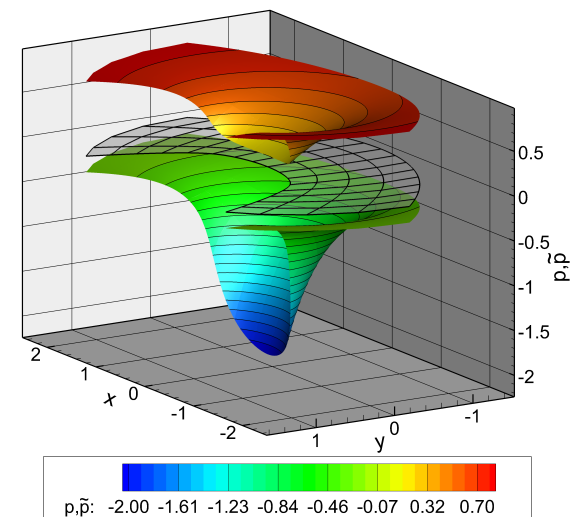
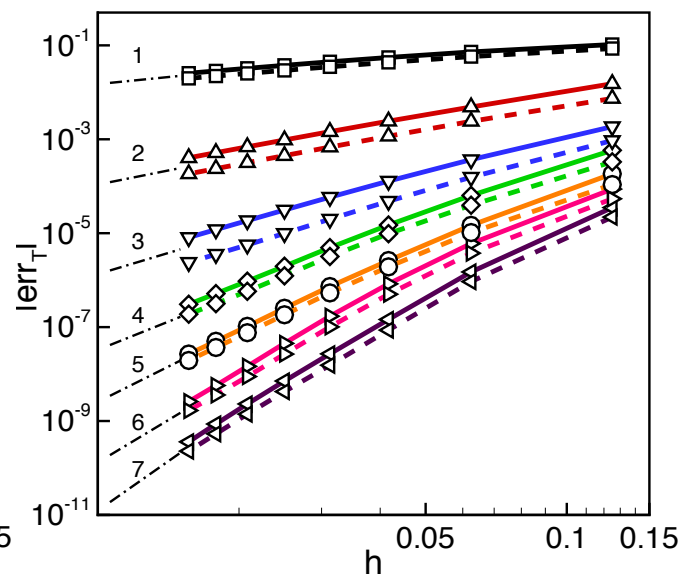
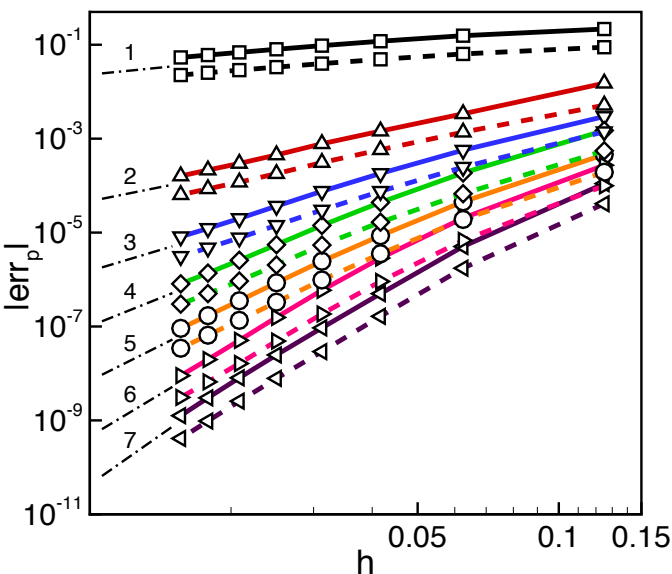
Working variables

Primitive variables to ensure the positivity of all thermodynamic variables at the discrete level....

We work with **polynomial approximations** not directly for p and T but for **their logarithms** $\tilde{p} = \log(p)$ and $\tilde{T} = \log(T)$

In this way the computed values $p = e^{\tilde{p}}$ and $T = e^{\tilde{T}}$ are always **positive**

Easy to implement: almost only change $\mathbf{M}_P$...



eXtra-Large Eddy Simulation (X-LES)

in a nutshell (I/II)

Pros

- hybrid RANS\LES formulation independent from the wall distance
- use in LES mode of a clearly defined SGS based on the k-equation
- use of a k- ω turbulence model integrated to the wall

Cons

the *filter width* parameter is often related to the local element size

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_j}(\rho u_j k) = \frac{\partial}{\partial x_j} \left[(\mu + \sigma^* \bar{\mu}_t) \frac{\partial k}{\partial x_j} \right] + P_k - D_k$$

$$\begin{aligned} \frac{\partial}{\partial t}(\rho \tilde{\omega}) + \frac{\partial}{\partial x_j}(\rho u_j \tilde{\omega}) &= \frac{\partial}{\partial x_j} \left[(\mu + \sigma \bar{\mu}_t) \frac{\partial \tilde{\omega}}{\partial x_j} \right] + (\mu + \sigma \bar{\mu}_t) \frac{\partial \tilde{\omega}}{\partial x_k} \frac{\partial \tilde{\omega}}{\partial x_k} \\ &+ P_\omega - D_\omega + C_D \end{aligned}$$

...an “original” interpretation for the X-LES implementation...

eXtra-Large Eddy Simulation (X-LES)

in a nutshell (II/II)

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_j}(\rho u_j k) = \frac{\partial}{\partial x_j} \left[(\mu + \sigma^* \bar{\mu}_t) \frac{\partial k}{\partial x_j} \right] + P_k - D_k$$

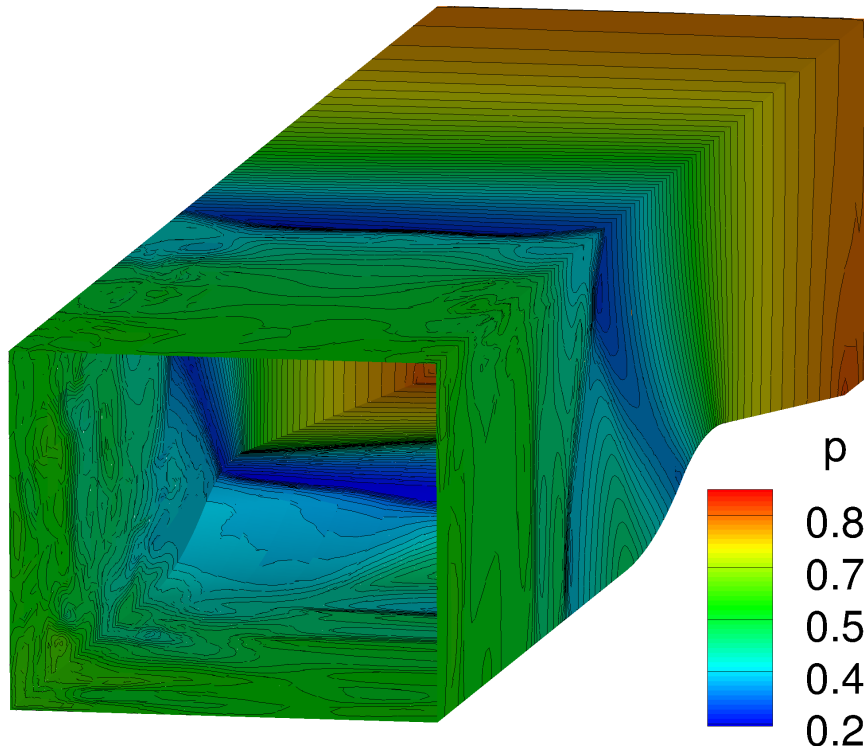
$$\bar{\mu}_t = \alpha^* \frac{\rho \bar{k}}{\hat{\omega}} \quad D_k = \beta^* \rho \bar{k} \hat{\omega} \quad \bar{k} = \max(0, k)$$

$$\hat{\omega} = \max \left(e^{\tilde{\omega}_r}, \frac{\sqrt{\bar{k}}}{C_1 \Delta} \right)$$

	RANS	LES	ILES
$\bar{\mu}_t$	$\alpha^* \frac{\rho \bar{k}}{e^{\tilde{\omega}_r}}$	$\alpha^* \rho \sqrt{\bar{k}} C_1 \Delta$	0
D_k	$\beta^* \rho \bar{k} e^{\tilde{\omega}_r}$	$\beta^* \rho \frac{\bar{k}^{\frac{3}{2}}}{C_1 \Delta}$	0

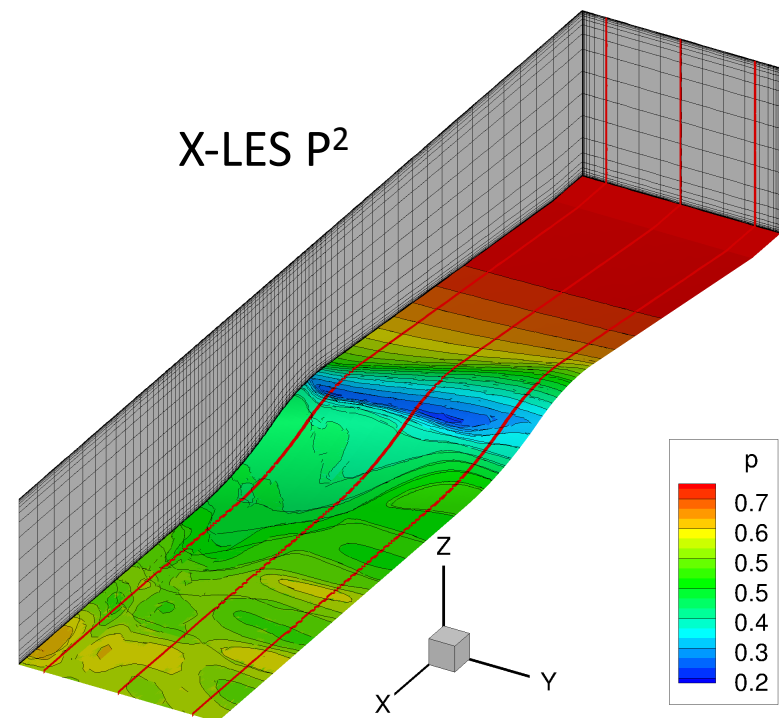
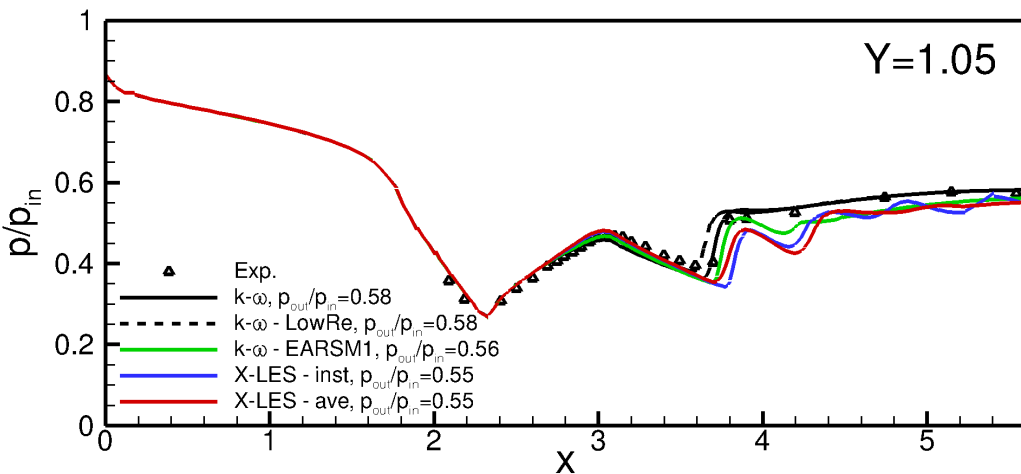
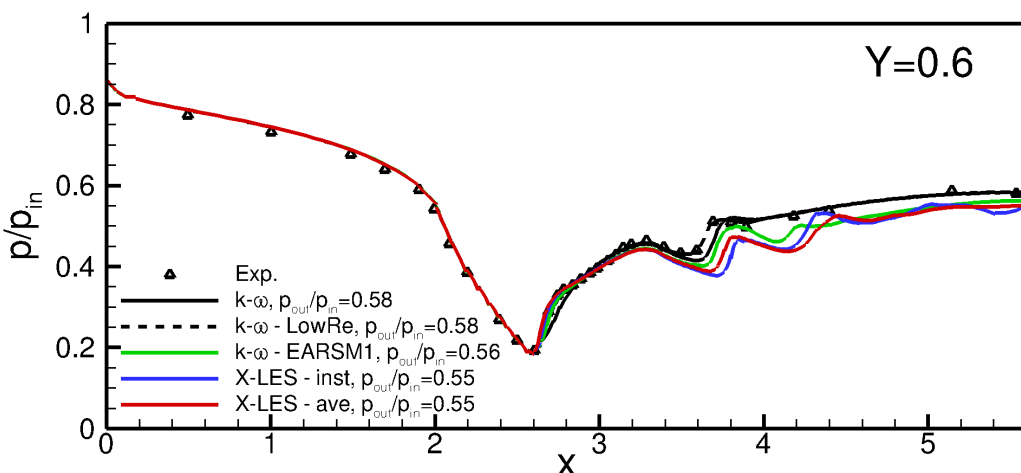
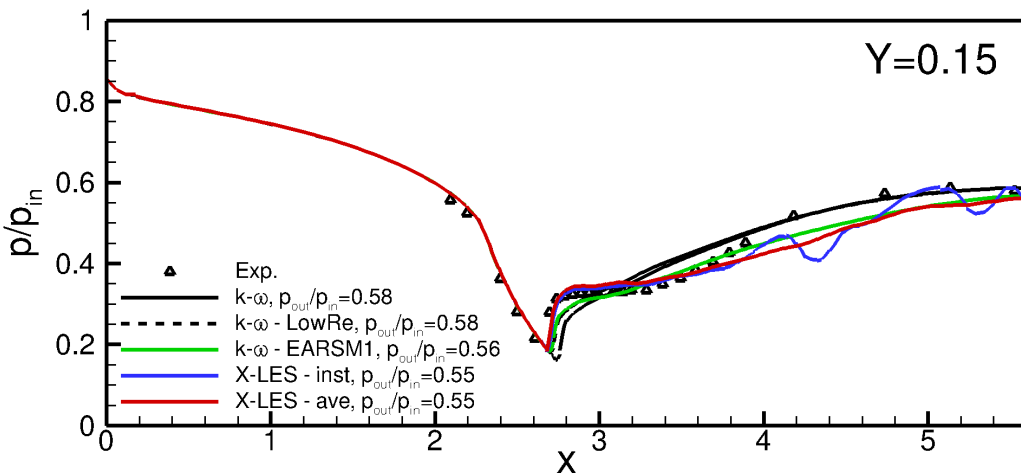
X-LES of a shock BL interaction on a swept bump (AR2)

P² converged computations with **RANS+k- ω** (also in its low-Re version) and **EARSM1** have been performed and used as **initialization** for **X-LES**

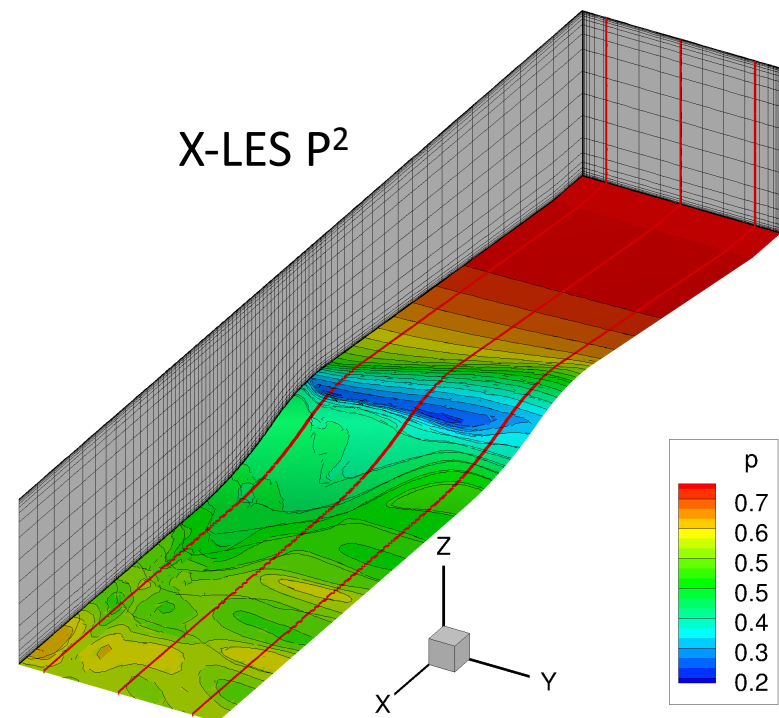
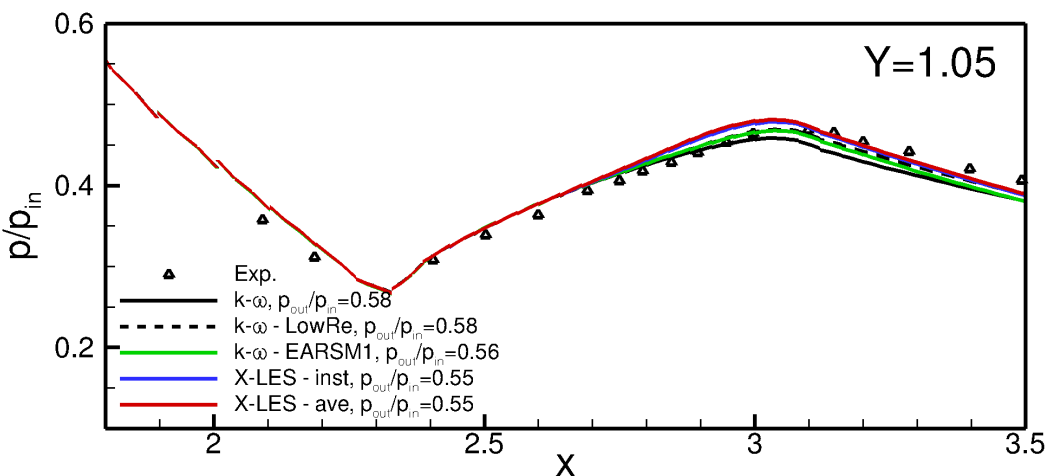
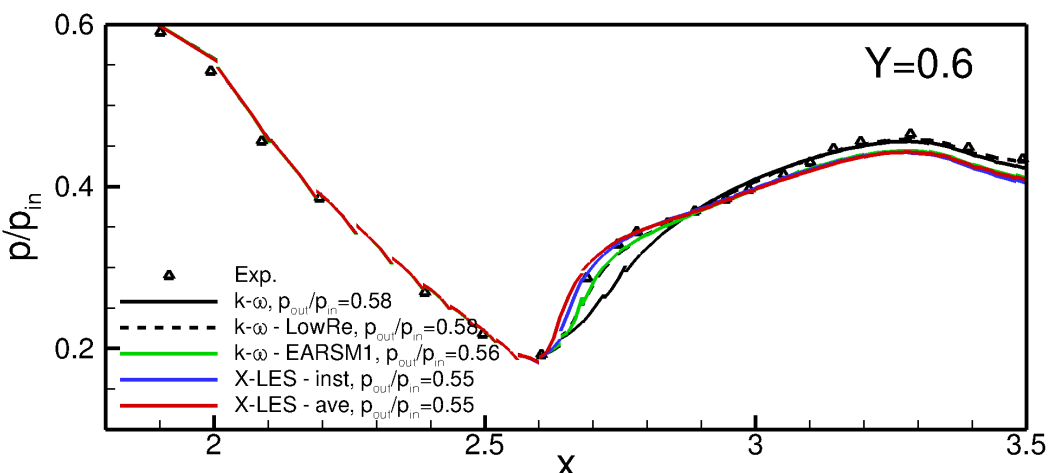
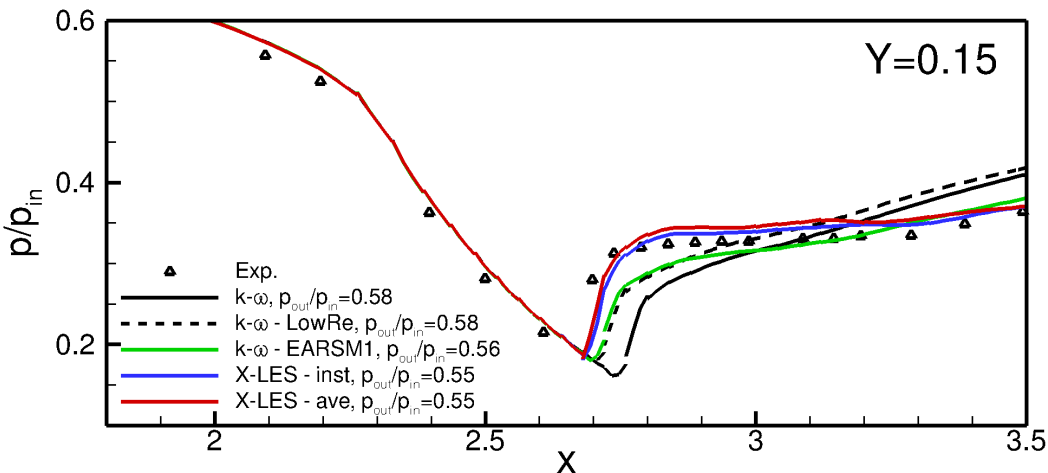


72960 hexahedral elements

- Inlet boundary conditions
 - $p_{0i} = 92000\text{Pa}$
 - $T_{0i} = 300\text{K}$
 - $Re_H = 1.69 \times 10^6$
- **Outlet static pressure** used to impose the **shock position (model dependent!)**
- LBE to quickly find the “right” pressure ratio
- RO3-3 for the time-accurate solution
- Filter width $\Delta = 5e-2$ (**strong influence!**)
- 96 cores of our in-house Intel cluster :-)

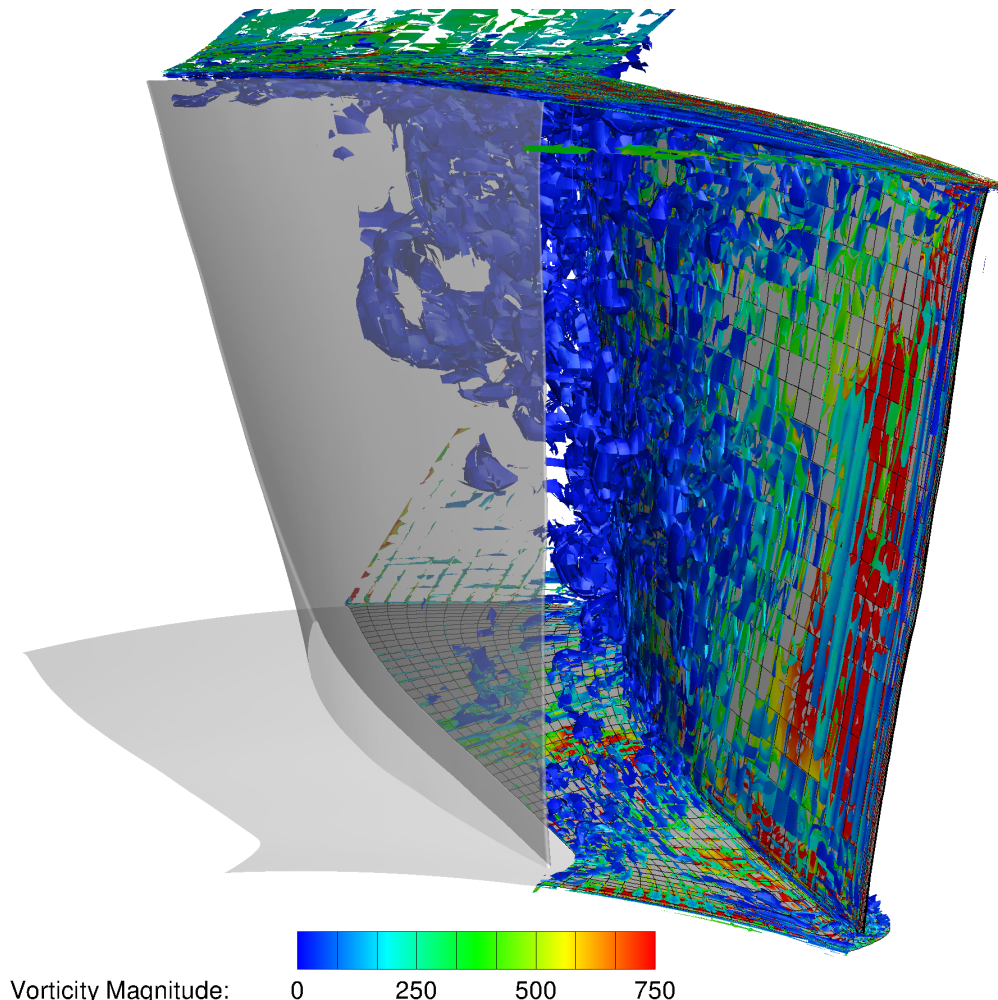


The profiles are in reasonable agreement with the experiments and the numerical results of Cahen et al.



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X-LES of the transonic flow field in the NASA Rotor 37



iso-surface of Q-criterion
160512 hexahedral elements

- P^2 computation using RO3-3
- Filter width $\Delta=5e-5$
- Boundary conditions
 - $p_{01} = 101325\text{Pa}$
 - $T_{01} = 288\text{K}$
 - $\omega = 1800\text{rad/s}$
 - $Tu_1 = 3\%$
 - $\alpha_1 = 0^\circ$
- still 96 cores of our in-house Intel cluster :-((

According to our first experiences, for a practical usage of X-LES, **initializing with RANS** seems mandatory

X-LES of the transonic flow field in the NASA Rotor 37

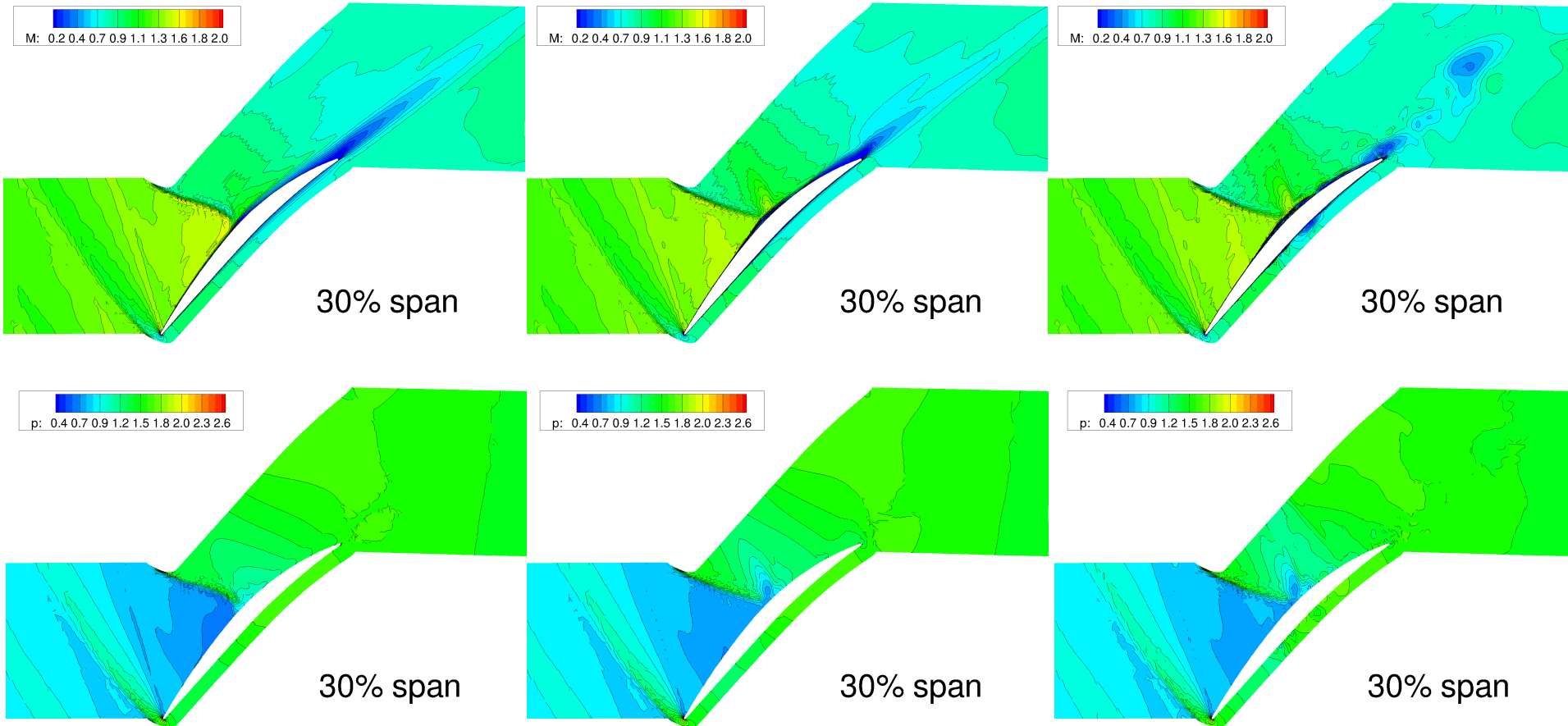


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RANS

X-LES ave.

X-LES inst.



X-LES of the transonic flow field in the NASA Rotor 37

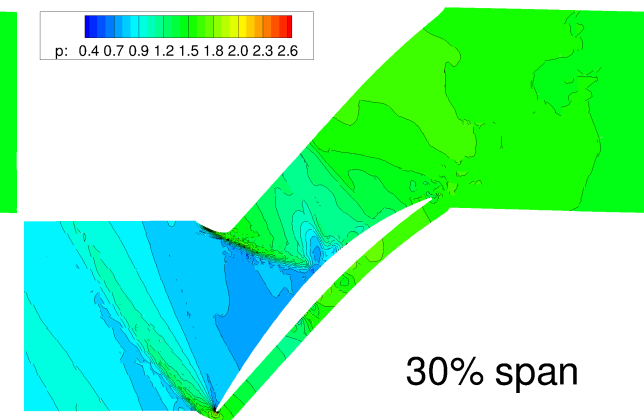
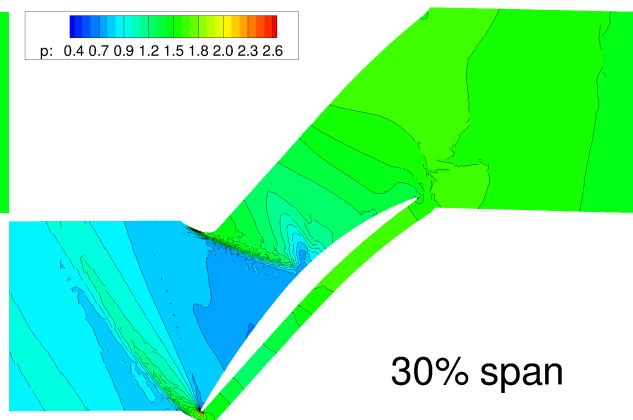
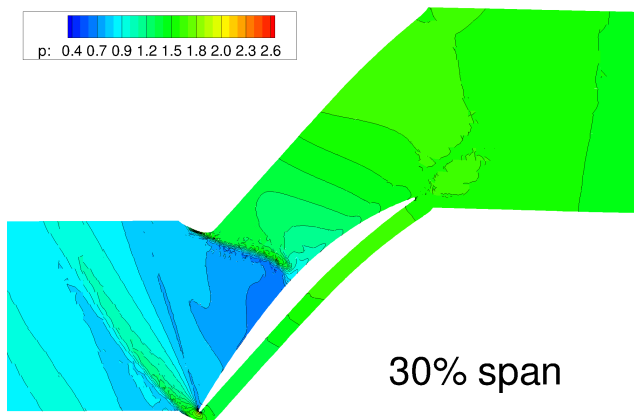
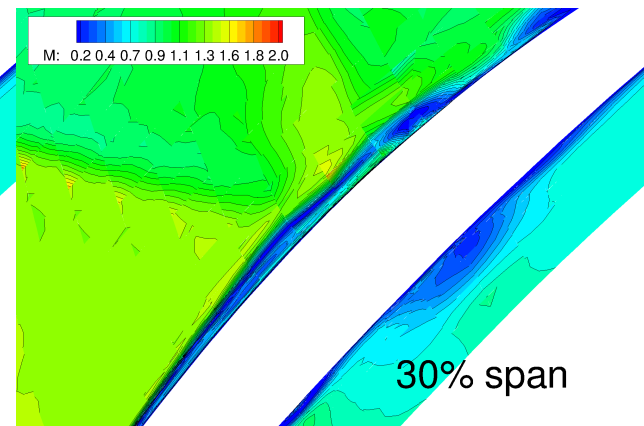
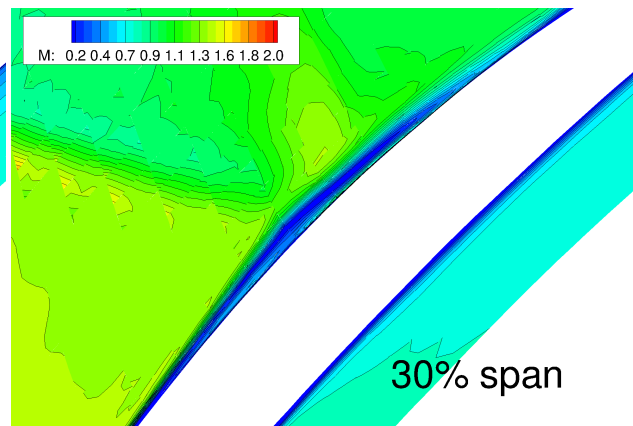
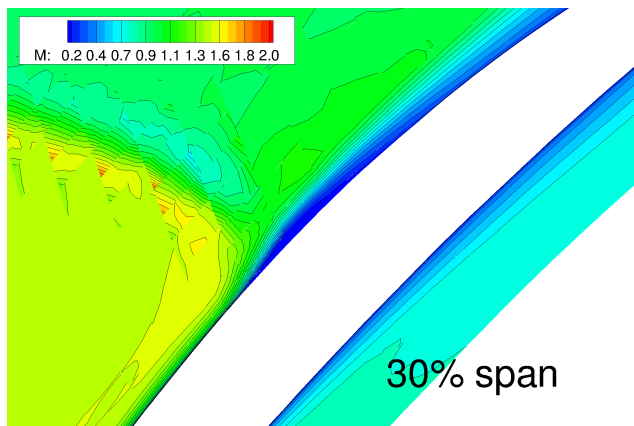


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RANS

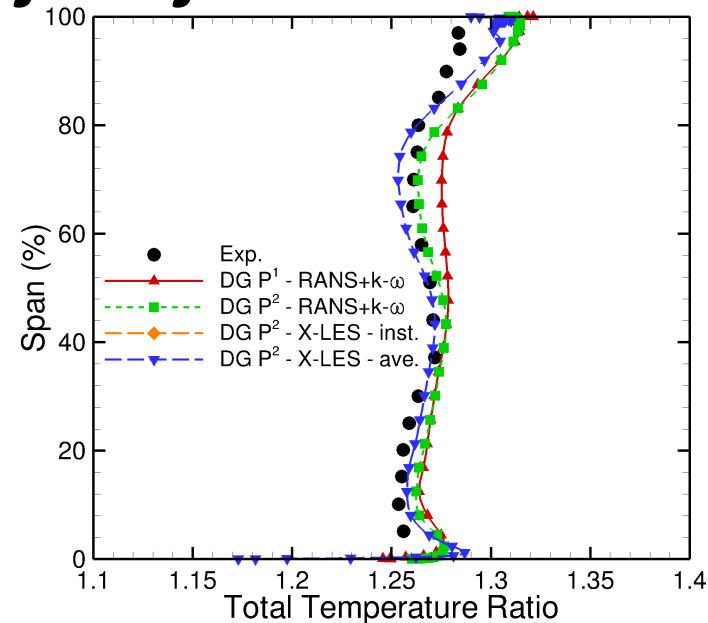
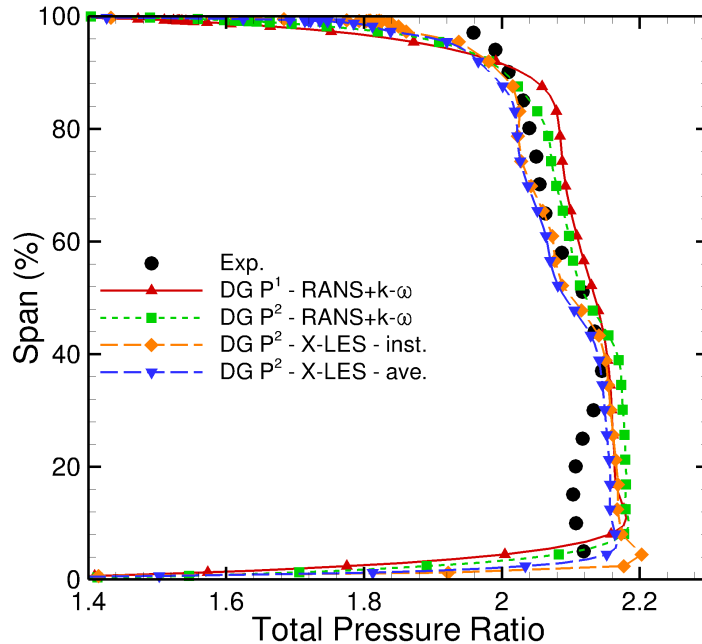
X-LES ave.

X-LES inst.

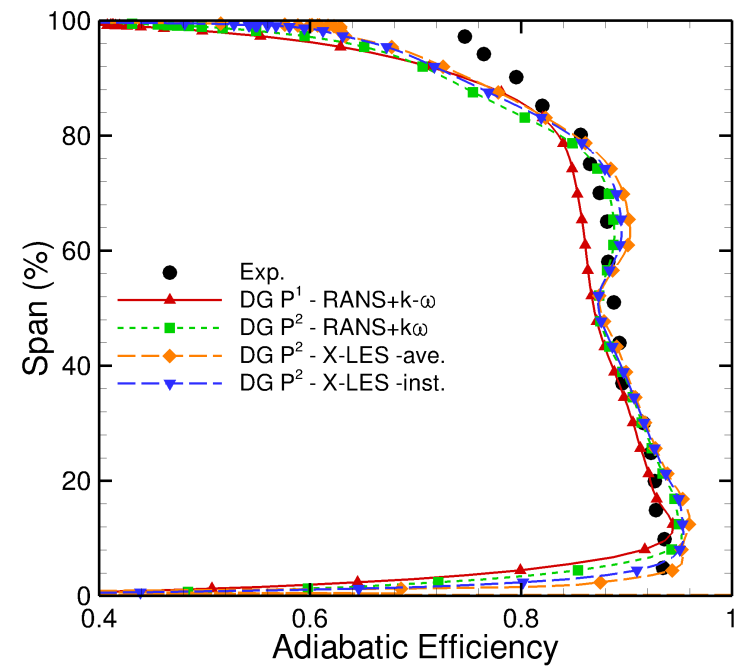


X-LES of the transonic flow field in the NASA Rotor 37

Spanwise distributions



Initializing the solution from a flow field
corresponding
to a normalized mass flow,
resulting from a **RANS** computation, of ≈ 0.98
X-LES moved towards ≈ 0.996



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Implicit time integration

Thursday, June 9 8:30-10:30 - MS 905 - 2 (Room 20)

Alessandra Nigro, Carmine De Bartolo, Andrea Crivellini, Francesco Bassi

**MATRIX-FREE MODIFIED EXTENDED BACKWARD DIFFERENTIATION FORMULAE
APPLIED TO THE DISCONTINUOUS GALERKIN SOLUTION OF COMPRESSIBLE UNSTEADY VISCOUS FLOWS**

Thursday, June 9 14:30-16:30 - MS 905 - 3 (Room 20)

*Francesco Carlo Massa, Gianmaria Noventa, Francesco Bassi, Alessandro Colombo,
Antonio Ghidoni, Marco Lorini*

**HIGH-ORDER LINEARLY IMPLICIT TWO-STEP PEER METHODS FOR
THE DISCONTINUOUS GALERKIN SOLUTION OF THE INCOMPRESSIBLE RANS EQUATIONS**

Thursday, June 9 17:00-19:00 - MS 905 - 4 (Room 20)

Antonio Ghidoni, Marco Lorini, Gianmaria Noventa, Francesco Bassi, Alessandro Colombo

**DISCONTINUOUS GALERKIN SOLUTION OF THE REYNOLDS- AVERAGED NAVIER-STOKES AND
KL-KT-LOG(W) TRANSITION MODEL EQUATIONS**

Friday, June 10 9:00-11:00 - MS 910 - 2 (Room 15)

*Francesco Bassi, Lorenzo Botti, Alessandro Colombo, Andrea Crivellini, Antonio Ghidoni,
Marco Lorini, Francesco Carlo Massa, Gianmaria Noventa*

ON THE IMPLEMENTATION OF X-LES IN A HIGH-ORDER IMPLICIT DG SOLVER

Turbulence Modeling

Tuesday, June 7 8:30-10:30 - CS 930 - 3 (Room 15)

Francesco Bassi, Alessandro Colombo, Andrea Crivellini, Matteo Franciolini

HYBRID OPENMP/MPI PARALLELIZATION OF A HIGH-ORDER DISCONTINUOUS GALERKIN CFD SOLVER

HPC